



ASQ CRE Prep course

Lesson II. A. 5. b.

Non-Parametric Methods

Ranking

A scenic view of a beach and ocean framed by a wooden structure. The sky is a deep blue with scattered white clouds. The ocean is a vibrant turquoise color, with white waves breaking on a sandy beach. A large, dark rock sits in the water near the shore. On the right, a red flag is visible on a pole. The wooden frame of the structure is visible on the left and top edges.

Powerful nonparametric techniques

NONPARAMETRIC TECHNIQUES

Kendall Coefficient of Concordance

- **Let's say three people ranked ordered their preference for 10 pieces of music.**
- **Determine if the three people like the same music (similar rank orders)**

Rankings (raw data)

A	B	C
1	7	6
5	6	4
6	2	8
7	5	5
10	9	10
4	3	1
8	1	3
3	10	9
9	4	7
2	8	2

Rank Sums(add across)

A	B	C
1	7	6
5	6	4
6	2	8
7	5	5
10	9	10
4	3	1
8	1	3
3	10	9
9	4	7
2	8	2

i	R_i
1	14
2	15
3	16
4	17
5	29
6	8
7	12
8	22
9	20
10	12

Some calculations

- **Determine R-bar**

$$\bar{R} = m(n + 1) / 2$$

- **m is number of evaluators**
- **n is number of items being ranked**
- **In this case R-bar is 16.5**

- **Compute S – sum of squared deviations**

$$S = \sum_{i=1}^n (R_i - \bar{R})^2$$

- **S = 320.5**

W Coefficient

- **Compute Kendall's coefficient of concordance, W**

$$W = \frac{12S}{m^2(n^3 - n)}$$

- **W = 0.432**

W is between zero (no concordance) and 1 (high concordance)

Test Statistic

- **Chi Squared value**

This is only for $n > 7$

$$W = \frac{12S}{mn(n+1)}$$

- **$\chi^2 \approx 11.65$**

Critical Value

- **For $n > 7$ use Chi-squared**
- **$df = n - 1$**
- **$\alpha = 0.1$
(using 90% confidence)**
- **From tables**
- **14.684**
- **Since the test statistic is less than critical value, 11.65. Insufficient evidence of alignment between rankings.**

Spearman Rank Correlation Coefficient

- **Determine degree of association between two ordered series.**
- **R_s approaches 1 or -1 for strong correlation and approaches 0 for weak correlation.**
- **Like ratings on movies**
- **Unknown distribution**

$$r_s = 1 - \left(\frac{6 \sum D^2}{n(n^2 - 1)} \right)$$

Kruskal-Wallis One-way Analysis of Variance by Ranks

- **Compare 3 or more groups or treatments**
- **Any or unknown distribution**
- **Data has to be suitable for ranking**
- **Comparing ranking, not actual data**
- **Hypothesis test structure**
- **Ranks in each group about the same – null**

See

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Non-Parametric Methods

Reliability & Comparisons