



# ASQ CRE Prep course

Lesson II. A. 4. e.

Poisson Process Models

Laplace's Trend Test





Another trend test

# LAPLACE'S TREND TEST

# Step 1: Set Period of Observation

- **Set T the period of interest**
- **Either at time of last failure**
  - Drop last failure and
  - Reduce n by one
- **Or, a duration of interest, say one year**

## **Step 2: Gather arrival times**

- **Test uses cumulative times, not interarrival times**
- **Let's use the example of:**

**36, 63, 86, 128, 165, 324**

**are days on which repairs occur  
and repairs take about an hour**



# Step 3: Calculate test statistic

- **The test statistic  $z$  is**

$$z = \left( \frac{2\bar{t}}{T} - 1 \right) \sqrt{3n}$$

- $T$  is selected duration

- $\bar{t}$  is the mean of cumulative time to failure data

$$\bar{t} = \frac{\sum t_i}{n} = \frac{802}{6} = 133.67$$

- **Let's set  $T = 365$  days, and**

- **Thus** 
$$z = \left( \frac{2\bar{t}}{T} - 1 \right) \sqrt{3n} = \left( \frac{2(133.67)}{365} - 1 \right) \sqrt{3(6)} = -1.135$$

# Step 5: Compare z-value & critical value

- **The critical value for  $\alpha = 0.05$  for this two sided test is  $\pm 1.96$**
- **Since  $-1.13$  is within the range of  $\pm 1.96$  the data does not show convincing evidence of a trend**
- **Extreme negative values show improving reliability, extreme positive values show degradation**

Why would you  
want to know  
the trend?



# ASQ CRE Prep course

Lesson II. A. 4. f.

Poisson Process Models

Fisher's Composite Test